Paul Pollack

Curriculum Vitae¹

University of Georgia

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POSITIONS HELD -

University of Illinois

J. L. Doob Research Assistant Professor/NSF Postdoctoral Fellow Fall 2008–Spring 2011

Institute for Advanced Study

Member of the School of Mathematics Fall 2009

Dartmouth College

Visiting Research Scholar Spring 2010

University of British Columbia/Simon Fraser University

Postdoctoral Fellow July 2011–April 2012

University of Georgia

Associate Professor Fall 2012-Summer 2016
Associate Professor Fall 2016-

Tibboolate Trotopol

EDUCATION -

University of Georgia

Bachelor of Science, Mathematics Spring 2003

Princeton University

Fall 2003 – Winter 2005

Dartmouth College

Master of Arts, Mathematics

Ph.D., Mathematics

June 2007

June 2008

Thesis: Prime polynomials over finite fields

HONORS AND AWARDS —

Sandy Beaver Excellence in Teaching Award

2018

Annual award honoring UGA Franklin College faculty members showing "sustained commitment to high-quality instruction".

NSF Algebra and Number Theory Award DMS-1402268

2014-2017

Statistical problems in elementary, analytic, and algebraic number theory (award amount \$130,925)

NSF Algebra and Number Theory Award DMS-1502336

(co-PI w/ L. Thompson, R. Rumely, and G. Yu)

Summer 2015

Conference grant for "Elementary, analytic, and algorithmic number theory: Research inspired by the mathematics of Carl Pomerance" (award amount \$19,728)

¹Last updated: February 15, 2018

NSA Conference Award (co-PI w/ L. Thompson, R. Rumely, and G. Yu)	Summer 2015
"Carl Pomerance 70th birthday conference" (award amount \$15,788)	
RECENT INVITED ADDRESSES —	
American Institute of Mathematics workshop on arithmetic statistics over finite fields and function fie 'On the distribution of irreducible polynomials vs. the distribution of ra	* .
2014 Illinois Number Theory conference in memory of the Batemans and Heini Halberstam 'Solved and unsolved problems in elementary number theory'	June 6, 2014
American Institute of Mathematics workshop on gaps between primes 'Big doings with small gaps'	November 19, 2014
CRM workshop on "New approaches in probabilistic and multiplicative number theory" 'Statistics associated with reductions of elliptic curves modulo p '	December 12, 2014
American Association for the Advancement of Science Annual Meropanelist for special session on gaps between primes 'Big doings with small gaps'	reting February 16, 2015
Math Honors Day, Mercer University 'Summing divisors: A status report on the first 2000 years'	March 19, 2015
Spring 2015 Southeastern Sectional Meeting of the AMS 'Big doings with small gaps' (one of 4 plenary talks)	March 27, 2015
2015 Illinois Number Theory conference 'Anatomy of torsion in the CM case'	August 14, 2015
2016 Gainesville International Number Theory conference 'Phi-nomenology and torsion subgroups of CM elliptic curves'	March 19, 2016
Analytic Number Theory workshop in Oberwolfach, Germany 'Torsion subgroups of CM elliptic curves'	November 12, 2016
2017 National Joint Meetings of the AMS and MAA; AMS special Structures in Number Theory"	session on "Discrete January 5, 2017
'Torsion subgroups of CM elliptic curves' MSRI workshop on "Recent developments in Analytic Number The 'Arithmetic functions: something old, something new'	heory" May 5, 2017
XII International Congress of Scientific Research, Dominican Rep 'Arithmetic functions: something old, something new'	ublic June 8, 2017
60th Anniversary Ross Mathematics Program reunion conference 'Summing divisors: a status report on the first 2000 years'	June 18, 2017
Invited address at Spring 2018 KYMAA meeting	April 6, 2018

'Summing divisors: a status report on the first 2000 years'

 ,	OCEI TED I AI ERS	
1.	An explicit approach to Hypothesis H for polynomials over a finite field The anatomy of integers. Proceedings of a conference on the anatomy of integers, Mc March 13th-17th, 2006. Editors: J.M. de Koninck, A. Granville and F. Luca, pp. 259–27	
2.	On a conjecture of Beard, O'Connell and West concerning perfect polynomials (joint with L. Gallardo and O. Rahavandrainy) Finite Fields and their Applications 14, 242–249	2008
3.	A polynomial analogue of the twin prime conjecture Proc. Amer. Math. Soc. 136, 3775–3784	2008
4.	Simultaneous prime specializations of polynomials over finite fields Proc. London Math. Soc. 97, 545–567	2008
5.	Arithmetic properties of polynomial specializations over finite fields Acta Arith. 136, 57-79	2009
6.	On the distribution of sociable numbers (w/ M. Kobayashi and C. Pomerance) $J.\ Number\ Theory\ 129,\ 1990-2009$	2009
7.	A remark on sociable numbers of odd order J. Number Theory 130, 1732–1736	2010
8.	Revisiting Gauss's analogue of the prime number theorem for polynomials over a finite field Finite Fields and their Applications 16, 290-299	2010
9.	Hypothesis H and an impossibility theorem of Ram Murty Rend. Sem. Mat. Univ. Pol. Torino 68, 183–197	2010
10	Multiperfect numbers with identical digits (joint with F. Luca) J. Number Theory 131, 260–284	2011
11.	On polynomial rings with a Goldbach property Amer. Math. Monthly 118, 71–77	2011
12.	On Dickson's theorem concerning odd perfect numbers Amer. Math. Monthly 118, 161–164	2011
13.	Long gaps between deficient numbers Acta Arith. 146, 33-42	2011
14.	On Hilbert's solution of Waring's problem Cent. Eur. J. Math. 9, 294–301	2011
15.	Powerful amicable numbers Colloq. Math. 122, 103–123	2011
16	Values of the Euler and Carmichael functions which are sums of three squares Integers 11, article A13, 16 pages (electronic)	2011
17.	On some friends of the sociable numbers Monatsh. Math. 162, 321–327	2011
18.	The greatest common divisor of a number and its sum of divisors	2011

Michigan Math. J. **60**, 199–214

19.	Perfect numbers with identical digits Integers 11A. Proceedings of the Integers Conference 2009. Article 18, 11 pages (electro	2011
20	Quasi-amicable numbers are rare	2011
20.	J. Integer Sequences 14, article 11.5.2, 13 pages (electronic)	2011
21.	The exceptional set in the polynomial Goldbach problem Int. J. Number Theory 7, 579–591	2011
22.	The Möbius transform and the infinitude of primes Elem. Math. 66, 118–120	2011
23.	Remarks on a paper of Ballot and Luca concerning prime divisors of $a^{f(n)}-1$ New York J. Math 17, 553–567	2011
24.	On common values of $\phi(n)$ and $\sigma(m)$, I (joint with K. Ford) Acta Math. Hungarica 133, 251–271	2011
25.	Two remarks on iterates of Euler's totient function Arch. Math. 97, 443-452	2011
26.	An arithmetic function arising from Carmichael's conjecture (w/ F. Luca) J. Théor. Nombres Bordeaux 23, 697–714	2011
27.	The average least quadratic nonresidue modulo m and other variations on a theme of Erdős J. Number Theory 132, 1185–1202	2012
28.	On the parity of the number of multiplicative partitions and related problems $Proc.\ Amer.\ Math.\ Soc.\ 140,\ 3793-3803$	2012
29.	On perfect and near-perfect numbers (joint with V. Shevelev) J. Number Theory 132, 3037–3046	2012
30.	Prime-perfect numbers (joint with C. Pomerance) Integers 12A/special issue in memory of J. L. Selfridge, article A14, 19 pages	2012
31.	Finiteness theorems for perfect numbers and their kin American Math. Monthly 119, 670–681	2012
32.	How many primes can divide the values of a polynomial? (joint with F. Luca) Acta Arith. 156, 19–27	2012
33.	On congruences of the form $\sigma(n) \equiv a \pmod{n}$ (with A. Anavi and C. Pomerance) Int. J. Number Theory 9, 115–124	2012
34.	On common values of $\phi(n)$ and $\sigma(m)$, II (joint with K. Ford) Algebra Number Theory 6, 1669–1696	2012
35.	The average least character nonresidue and further variations on a theme of Erdős (joint with G. Martin) J. London Math. Soc. 87, 22–42	2013
36.	On the degrees of divisors of $T^n - 1$ (joint with L. Thompson) New York J. Math 19, 91–116	2013
37.	Irreducible polynomials with several prescribed coefficients Finite Fields and their Applications 22, 70–78	2013

38.	Practical pretenders (joint with L. Thompson) Publ. Math. Debrecen 82, 651–667	2013
39.	Sets of monotonicity for Euler's totient function (w/ C. Pomerance and E. Treviño) Ramanujan J. 30, 379–398	2013
40.	On Mertens' theorem or Beurling primes Canad. Math. Bull. 56, 829–843	2013
41.	On the distribution of some integers related to perfect and amicable numbers (joint with C. Pomerance) Colloq. Math. 30, 169–182	2013
42.	The smallest inert prime in a cyclic number field of prime degree Math. Res. Lett. 20, 163–179	2013
43.	Paul Erdős and the rise of statistical thinking in elementary number theory (joint with C. Pomerance) Erdős Centennial, L. Lovász, I.Z. Ruzsa, and V.T. Sós, eds., János Bolyai Math. Soc Springer-Verlag, Hungary, 2013, pp. 515–523	2013 e. and
44.	Uncertainty principles connected with the Möbius inversion formula (with C. Sanna) Bull. Aust. Math. Soc. 88, 460–472	2013
45.	Equidistribution mod q of abundant and deficient numbers Uniform Distribution Theory 9, 99–114	2014
46.	A remark on prime divisors of partition functions Int. J. Number Theory 10, 125–131	2014
47.	The error term in the count of abundant numbers (joint with M. Kobayashi) ${\it Mathematika~60,~43-65}$	2014
48.	The smallest prime that splits completely in an abelian number field <i>Proc. Amer. Math. Soc.</i> 142 , 1925–1934	2014
49.	Square values of Euler's function (joint with C. Pomerance) Bull. London Math. Soc. 46, 403–414	2014
50.	The primes that Euclid forgot (joint with E. Treviño) Amer. Math. Monthly 121, 433–437	2014
51.	Variations on a theorem of Davenport concerning abundant numbers (w/ E. Jennings and L. Thompson) Bull. Aust. Math. Soc. 89, 437–450	2014
52.	Prime splitting in abelian number fields and linear combinations of Dirichlet characters Int. J. Number Theory 10, 885–903	2014
53.	Averages of the number of points on elliptic curves (w/ G. Martin and E. Smith) Algebra Number Theory $\bf 8,813-836$	2014
54.	Bounded gaps between primes with a given primitive root Algebra Number Theory 8, 1769–1786	2014

55.	Some arithmetic properties of the sum of proper divisors and the sum of prime divisors **Illinois J. Math 58, 125–147*	2014
56.	Euler and the partial sums of the prime harmonic series Elem. Math. 70, 13–20	2015
57.	Bounded gaps between primes in number fields and function fields (with A. Castillo, C. Hall, R. Lemke Oliver, and L. Thompson) Proc. Amer. Math. Soc. 143, 2841–2856	2015
58.	An easy generalization of Euler's theorem on the series of prime reciprocals American Math. Monthly 122, 159–163	2015
59.	Some normal numbers generated by arithmetic functions (with J. Vandehey) Canad. Math. Bull. 58, 160–173	2015
60.	The truth about torsion in the CM case (with P. L. Clark) C. R. Math. Acad. Sci. Paris 353, 683–688	2015
61.	Palindromic sums of proper divisors Integers 15A/Proceedings of the Erdős Centennial Conference, article A13 (electronic), 12 pages	2015
62.	Harmonious pairs (joint with M. Kozek, F. Luca, and C. Pomerance) Int. J. Number Theory 11, 1633–1651	2015
63.	Arithmetic functions at consecutive shifted primes (with L. Thompson) Int. J. Number Theory 11, 1477–1498	2015
64.	The length spectra of arithmetic hyperbolic 3-manifolds and their totally geodesic surfaces (with B. Linowitz and J. S. Meyer) New York J. Math 21, 955-972	2015
65.	Besicovitch, bisection, and the normality of 0.1491625 (with J. Vandehey) American Math. Monthly 122, 757–765	2015
66.	Remarks on fibers of the sum-of-divisors function in Analytic Number Theory: In Honor of Helmut Maiers 60th Birthday, M. Rassias a Pomerance, eds., Springer, 305–320	2015 and C
67.	On relatively prime amicable pairs Mosc. J. Comb. Number Theory 5, 36–51	2015
68.	The average of the first invariant factor for reductions of CM elliptic curves mod p (with T. Freiberg) Int. Math. Res. Notices 2015, no. 21, 11333–11350	2015
69.	Some problems of Erdős on the sum-of-divisors function (joint with C. Pomerance) Trans. Amer. Math. Soc. Ser. B. 3, 1–26	2016
70.	A Titchmarsh divisor problem for elliptic curves Math. Proc. Cambridge Philos. Soc. 160, 167–189	2016
71.	A remark on divisor weighted sums Ramanujan J. 40, 63–69	2016
72.	Bounded gaps between primes with a given primitive root, II (w/ R. C. Baker) Forum Mathematicum. 28, 675–687	2016

73.	Digitally delicate primes (w/ J. Hopper) J. Number Theory 168, 247–256	2016
74.	The representation function for sums of three squares along arithmetic progressions Proc. Japan Acad., Ser. A Math. Sci. 92, 96–99	2016
75.	An elemental Erdős-Kac theorem for algebraic number fields Proc. Amer. Math. Soc. 145, 971–987	2017
76.	Extremal primes for elliptic curves with complex multiplication (w/ K. James) $J.\ Number\ Theory\ {\bf 172},\ 383-391$	2017
77.	Anatomy of torsion in the CM case (with A. Bourdon and P. L. Clark) Math. Z. 285, 795–820	2017
78.	Bounds for the first several prime character nonresidues Proc. Amer. Math. Soc. 145, 2815–2826	2017
79.	A simple proof of a theorem of Hajdu–Jarden–Narkiewicz Colloq. Math. 147, 217–220	2017
80.	Two problems concerning irreducible elements in rings of integers of number field (w/ L. Troupe) Bull. Aust. Math. Soc. $\bf 96$, 44–58	elds 2017
81.	Counting perfect polynomials (w/ U. Caner Cengiz and E. Treviño) Finite Fields and their Applications 47, 242–255	2017
82.	Clustering of linear combinations of multiplicative functions (w/ N. Lebowitz-Lockard) J. Number Theory 180, 660–672	2017
83.	Subgroup avoidance for primes dividing the values of a polynomial Rocky Mountain J. Math 47, 2043–2050	2017
84.	Numbers divisible by a large shifted prime and large torsion subgroups of CM e curves (w/ N. McNew and C. Pomerance) Int. Math. Res. Notices 2017 , $5525-5553$	lliptic 2017
85.	Torsion subgroups of CM elliptic curves over odd degree number fields (w/ A. Bourdon) Int. Math. Res. Notices 2017, 4923–4961	2017
86.	Clusters of primes with square-free translates (w/ R. C. Baker) Revista Mat. Iberoam. 33, 809–829	2017
87.	Bounded gaps between primes and the length spectra of arithmetic hyperbolic 3-orbifolds (w/ B. Linowitz, D. B. McReynolds, and L. Thompson) C. R. Math. Acad. Sci. Paris 355, 1121–1126	2017
88.	The number of atoms in a primefree atomic domain (w/ P. L. Clark and S. Gosavi) Comm. Algebra 45, 5431–5442	2017
89.	Eigenvalues of the Laplacian on domains with fractal boundary (w/ C. Pomerance) Horizons of Fractal Geometry and Complex Dimensions,, San Luis Obispo, June, 2016, Niemeyer, E. P. J. Pearse, J. A. Rock, and T. Samuel, eds. (to appear)	2018+ R. G.

2017

90.	Systoles of arithmetic hyperbolic surfaces and 3-manifolds (w/ B. Linowitz, D. B. McReynolds, and L. Thompson) Math. Res. Lett. (to appear)	2018+
01	The truth about torsion in the CM case, II (w/ P. L. Clark)	2018+
91.	Quart. J. Math. (to appear)	2010+
92.	Refinements of Lagrange's four-square theorem (w/ L. Goldmakher) $Amer.\ Math.\ Monthly$ (to appear)	2018+
93.	Thue's lemma in $\mathbb{Z}[i]$ and Lagrange's four-square theorem <i>Elem. Math.</i> (to appear)	2018+
94.	Divisor-sum fibers (w/ C. Pomerance and L. Thompson) Mathematika (to appear)	2018+
95.	Finding the four squares in Lagrange's theorem (w/ E. Treviño) Integers (to appear)	2018+
96.	Dirichlet's proof of the three-square theorem: an algorithmic perspective $(w/\ P.\ Schorn)$	2018+
	Math. Comp. (to appear)	
97.	Pursuing polynomial bounds on torsion (w/ P. L. Clark) Israel J. Math. (to appear)	2018+
98.	A note on Golomb topologies (w/ N. Lebowitz Lockard and P. L. Clark) Quaestiones Math. (to appear)	2018+
99.	The least prime quadratic nonresidue in a prescribed residue class mod 4 J. Number Theory (to appear)	2018+
100	. A remark on the number field analogue of Waring's constant $g(k)$ $\mathit{Math. Nachr.}$ (to appear)	2018+
SU	BMITTED PAPERS —	
	ounting and effective rigidity in algebra and geometry (joint with B. Linowitz, D.B. McReynolds, and L. Thompson)	
	note on the least prime that splits completely in a nonabelian Galois number (w/ Z. Ge and M. Milinovich)	field
Ту	vpically bounding torsion (w/ P. L. Clark and M. Milosevic)	
W	aring's problem for integral quaternions	
Sn	nall prime k th power residues for $k=2,3,4$: a reciprocity laws approach (w/ K	. Benli)
	onnegative multiplicative functions on sifted sets, and the square roots of -1 modulo shifted primes	
вс	OOKS —	
	Not always buried deep: A second course in elementary number theory American Mathematical Society	2009

A conversational introduction to algebraic number theory

American Mathematical Society

SYNERGISTIC ACTIVITIES

Editorial positions

Associate Editor for the American Mathematical Monthly (2016 – 2022). Editor for the International Journal of Number Theory (2017–2019).

Refereeing

Have refereed for Acta Arith., Algebra Number Theory, Amer. Math. Monthly, Bol. Soc. Mat. Mexicana, Bull. Aust. Math. Soc., Bull. Brazilian Math. Soc., Bull. Korean Math. Soc., Canad. Math. Bull., Canad. J. Math., Exp. Math., Integers, Int. J. Number Theory, Int. Math. Res. Notices, J. Integer Sequences, J. Logical and Algebraic Methods in Programming, J. Number Theory, J. Combinatorics and Number Theory, Math. Comp., Mathematika, and the Handbook of Finite Fields.

Have refereed grant proposals for the National Security Administration. Served on National Science Foundation grant panels in 2015 and 2017.

Special session organizer

Co-organized (with L. Goldmakher, M. Milinovich, J. Kish) a special session at the 2012 AMS/MAA Joint Meetings titled "New perspectives on multiplicative number theory." This was a special session following up on an NSF-sponsored Mathematics Research Communities workshop ("The pretentious view of analytic number theory").

For the 2014 Joint Meetings, co-organized (with C. Pomerance) an MAA Invited Paper Session titled "The continuing influence of Paul Erdős in number theory".

Organized the special session "Elementary methods in analytic number theory" at the Spring 2015 Southeastern AMS Sectional Meeting in Huntsville, AL (March 27–29, 2015).

Organized (with R. Lemke Oliver and F. Thorne) a special session for the 2017 AMS/MAA Joint Meetings titled "Analytic number theory and arithmetic" (January 7, 2017).

Work with junior mathematicians

Since 2001, the University of Georgia has organized a high school math tournament for students in Georgia and neighboring states. Since 2012, I have served as one of the primary contest organizers. In addition, in the summers of 2013, 2014, and 2016, I was a faculty mentor for the week-long UGA MathCamp organized by Angela Gibney and Danny Krashen. (There was no camp in 2015 or 2017.)

Served on a Young Mathematicians' Network panel at the 2016 AMS/MAA Joint Meetings. The subject was "Finding a thesis topic and advisor." Co-panelist with Allison Henrich of Seattle University.

Was one of 11 speakers at the 60th anniversary Ross Program reunion conference in June 2017. The Ross Program is a residential summer camp where high school students are immersed in the process of mathematical discovery for six weeks.

Will be co-running the Ross Math Asia Program in China, Summer 2018 (jointly with Enrique Treviño, Lake Forest College).

Teaching in developing countries

Taught a one-week course in Manila in July, 2013 for a summer school on algebraic curves. The summer school was sponsored by CIMPA (International Centre for Pure and Applied Mathematics) and ICTP (the Abdus Salam International Centre for Theoretical Physics); both of these are organizations aiming to promote scientific education in the developing world.

Taught a minicourse titled "Vistas in Number Theory", June 5–7, 2017, at the Universidad Autónoma de Santo Domingo in the Dominican Republic. This was one of four minicourses offered at UASD as a lead-in to an international scientific congress held later that week. The course introduced students and local faculty to central topics in elementary number theory.

MENTORING -

Postdoctoral mentor

Lola Thompson (2012–2013) Joseph Vandehey (2013–2016)

Thesis supervisor

Emily Jennings (M.A., 2014) Lee Troupe (Ph.D., Spring 2016) Kubra Benli (Ph.D., in progress) Noah Lebowitz-Lockard (Ph.D., in progress)

Undergraduate research supervisor (through UGA's Center for Undergraduate Research Opportunities)

Jackson Douglas Hopper (Spring 2015–present); Jackson received a \$1000 CURO research assistantship in Spring 2015 and a \$3000 CURO summer fellowship in Summer 2015. Our work on "digitally delicate" primes appeared in the Journal of Number Theory (paper #73 above).

UGA TEACHING EXPERIENCE -

Math 2260: Calculus II for science and engineering	Fall 2012
Math 3220: Advanced problem solving	Fall 2012
Math 3100: Sequences and series	Spring 2013
Math 4400/6400: Elementary number theory	Spring 2013
Math 3220: Advanced problem solving	Fall 2013
Math 8440: Advanced topics in elementary number theory	Fall 2013
Math 3100: Sequences and series	Spring 2014
Math 3220: Advanced problem solving	Fall 2014
Math 4150: Complex variables	Fall 2014
Math 3100H: Sequences and series (Honors)	Spring 2015
Math 3220: Advanced problem solving	Fall 2015
Math 4000: Modern algebra and geometry I	Fall 2015
Math 8850: Introduction to mathematical research (joint w/ P. L. Clark)	Fall 2015
Math 3100H: Sequences and series (Honors)	Spring 2016
Math 8400: Algebraic number theory	Spring 2016
Math 8850: Introduction to mathematical research (joint w/ P. L. Clark)	Spring 2016
Math 3220: Advanced problem solving	Fall 2016
Math 4000: Modern algebra and geometry I	Fall 2016
Math 3100H: Sequences and series (Honors)	Spring 2017
Math 4400/6400: Elementary number theory	Spring 2017
Math 3100: Sequences and series	Fall 2017
Math 3220: Advanced problem solving	Fall 2017
Math 8400: Algebraic number theory	Fall 2017
Math 3220: Advanced problem solving	Fall 2017
Math 8400: Algebraic number theory	Fall 2017
Math 4000: Modern algebra and geometry I	Spring 2018