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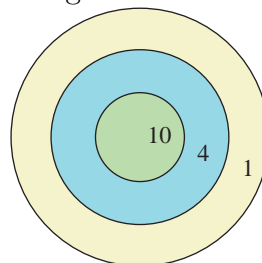
Problem 5. Express in terms of the fewest number of square roots possible:

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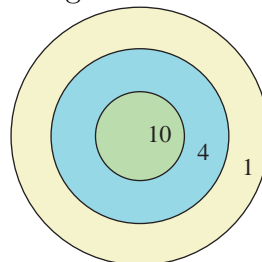
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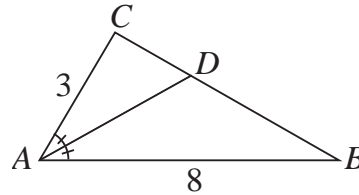
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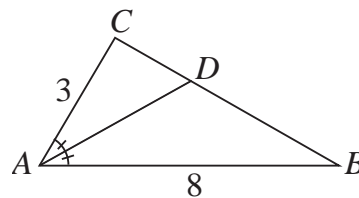
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