

Do not write in the boxes immediately below.

|           |    |    |    |    |    |    |       |
|-----------|----|----|----|----|----|----|-------|
| Question: | 1  | 2  | 3  | 4  | 5  | 6  | Total |
| Points:   | 36 | 10 | 10 | 10 | 16 | 18 | 100   |
| Score:    |    |    |    |    |    |    |       |

## MATH 2250 Exam 4

April 24, 2008

Name: \_\_\_\_\_

1. (36 points) Evaluate the following:

(a)  $\int \left( \frac{x^2 + 1}{4} - \frac{4}{x^2 + 1} \right) dx$

(b)  $\int_0^{\pi/16} \sec^2(4x) dx$

(c)  $\int_1^2 2x \left( \frac{x^2 + 3}{x^2} \right) dx$

2. (10 points) For each of the following, answer True or False:

(a)  $\lim_{x \rightarrow 3} \left( \frac{x - 3}{x^2 - 3} \right) = \lim_{x \rightarrow 3} \left( \frac{1}{2x} \right) = \frac{1}{6}$ .

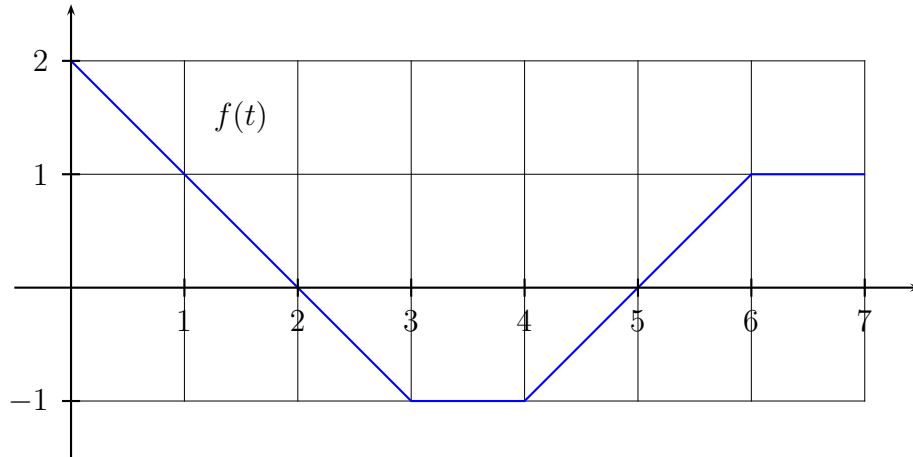
(b) For any function  $f(x)$ , there is at most one function  $F(x)$  such that  $F'(x) = f(x)$ .

3. (10 points) Let  $f(x) = \int_2^{\ln x} (t + 1) \cos(t^2) dt$ . Find  $f'(x)$ .

4. (10 points) Approximate  $\int_{-1}^1 x^3 dx$  by using a Riemann sum with  $n = 4$  and left endpoints.

5. (16 points) Evaluate  $\lim_{x \rightarrow 0} (\cos x - \sin x)^{2/\sin x}$ .

6. (18 points) Let  $f(t)$  be the function whose graph is shown below, and let  $g(x) = \int_1^x f(t) dt$ .



Compute the following:

(a)  $\int_1^6 f(t) dt$

(b)  $\int_1^0 f(t) dt$

(c)  $g'(2)$

(d)  $g'(4)$