By providing my signature below, I acknowledge that I abide by the University's academic honesty policy. This is my work, and I did not get any help from anyone else:

Name (sign): _____ Name (print): _____

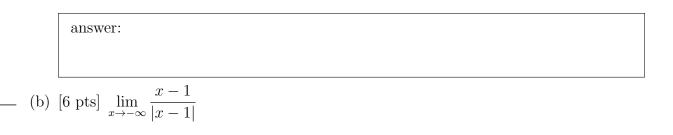
Class Time:

Student Number:

Instructor's Name:

- If you need extra space use the last page. Do not tear off the last page!
- Please show your work. An unjustified answer may receive little or no credit.
- If you make use of a theorem to justify a conclusion, then state the theorem used by name.
- Your work must be **neat**. If I can't read it (or can't find it), I can't grade it.
- The total number of possible points that is assigned for each problem is shown here. The number of points for each subproblem is shown within the exam.
- You may not use a cell phone or smart watch. Please turn off your cell phones and store them and your smart watches away from your desk or table.
- You are only allowed to use a **TI-30XS Multiview** calculator. No other calculators are permitted, and sharing of calculators is not permitted.
- You do not have to use a calculator; answers containing symbolic expressions such as cos(π/3) and ln(e⁴) are acceptable. Include an exact answer for each problem.

- 1. Determine the following limits; briefly explain your thinking on parts (b) and (c). If you apply L'Hopital's rule, indicate where you have applied it and why you can apply it. Print your final answer in the box provided.
 - (a) [6 pts] no explanation needed: $\lim_{x \to -1} (x^7 4x + 2)$





answer:			

2. [10 pts] Determine whether the function below is continuous at x = 3. Use the definition of continuity to explain your answer.

$$f(x) = \begin{cases} 4x - 6 & \text{if } x \le 3\\ \frac{\sqrt{x} - \sqrt{3}}{x - 3} & \text{if } x > 3 \end{cases}$$

3. (a) [5 pts] State the limit definition of the derivative of f(x).

(b) [10 pts] Use the <u>limit definition of the derivative</u> to determine the derivative of $f(x) = \frac{1}{1+2x}$. (No points will be awarded for the application of differentiation rules.)

4. Determine the first derivative of each of the following functions. Print your answer in the box provided. You do not have to simplify your answers or explain your steps.

(a) [6 pts]
$$f(x) = 7x^5 - x^{3/5} + 2018$$

(b) [6 pts]
$$g(x) = \frac{e^x}{x^2 + 5}$$

$$g'(x) =$$

(c) [8 pts] $f(x) = x^9 \cos(4x)$

f'(x) =

(d) [8 pts] $f(x) = \arctan(x) + \sqrt{x^7 + 3x}$

$$f'(x) =$$

5. (a) [10 pts] Determine $\frac{dy}{dx}$ where $2x^3 + 3x^2y + y^3 = 4$. Print your answer in the box provided. You do not have to simplify your answer.

 $\frac{dy}{dx} =$

(b) [5 pts] Determine all points on the graph of $2x^3 + 3x^2y + y^3 = 4$ at which the curve has a horizontal tangent line. Give your answer(s) in the form (x, y). (You may use your work from part (a).)

Answer:

6. Determine the following indefinite integrals. Print your answer to each part in the box provided. You do not have to simplify your answers or explain your steps.

(a) [6 pts]
$$\int (x^3 - 7x + 12) dx$$

Final answer:

(b) [6 pts]
$$\int \left(\frac{1}{\sqrt{1-x^2}} + \sec(x)\tan(x)\right) dx$$

Final answer:

(c) [8 pts]
$$\int e^{\sin(3x)}(\cos(3x)) dx$$

Final answer:

7. Evaluate the following definite integrals. Print your answer in the box provided. You do not have to simplify your answers or explain your steps.

- (a) [6 pts]
$$\int_0^{1/2} (e^x - \cos(\pi x)) dx$$

Value:
- (b) [8 pts]
$$\int_0^1 \left(\frac{1}{x^6 - 4x + 7}\right) (6x^5 - 4) dx$$

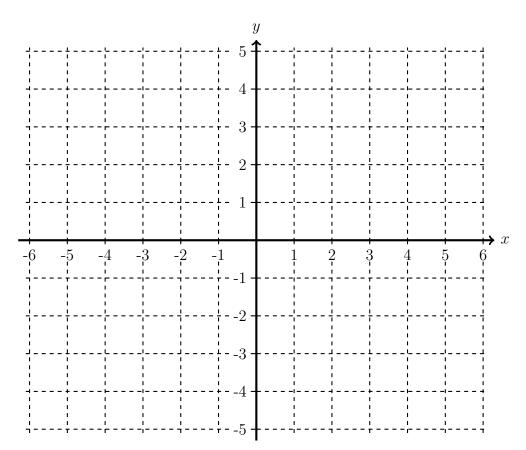
Value:

8. [10 pts] Use calculus to determine the absolute maximum and absolute minimum values of the function below on the interval [1, 5]:

$$f(x) = x^3(x-4)^3$$

9. [14 pts] Sketch the graph of a function f satisfying all of the following properties:

- The domain of f is $[-6, -1) \cup (-1, 3) \cup (3, 6]$
- $\lim_{x \to -1} f(x) = 1$
- $\lim_{x \to 3^{-}} f(x) = \infty$ and $\lim_{x \to 3^{+}} f(x) = 2$
- f(-4) = -1 and f(2) = -2
- f is continuous at every point in its domain
- The increasing/decreasing behavior of f is given in the following table:



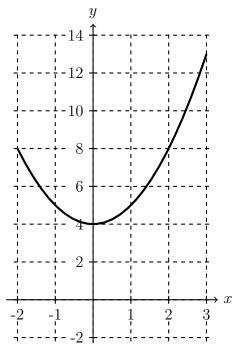
- 10. Consider the function $f(x) = e^{x^2}$.
 - (a) [10 pts] Determine interval(s) on which f is increasing and interval(s) on which f is decreasing.

(b) [6 pts] Approximate the integral $\int_{1}^{3} f(x) dx$ by a Riemann sum using four sub-intervals of equal width and left endpoints. You <u>do not</u> need to simplify your expression for the Riemann sum; expressions involving powers of e such as $e^{\sqrt{2}}$ are acceptable.

(c) [4 pts] Based <u>only</u> on your answer to part (a), will your final answer to (b) be an over-estimate or under-estimate of the true exact value of $\int_{1}^{3} f(x) dx$? Explain briefly.

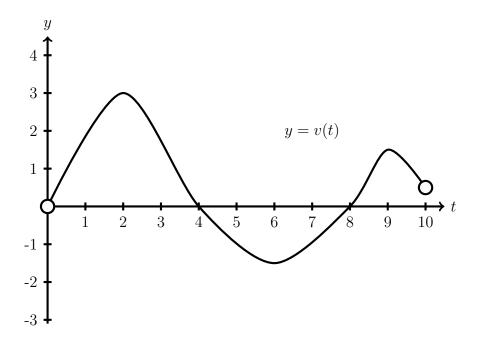
- 11. Consider the function $g(x) = x^2 + 4$.
 - (a) [8 pts] Determine the linearization L(x) of g(x) at x = 2.

(b) [4 pts] Sketch the graph of y = L(x) on the graph of y = g(x) below.



(c) [4 pts] Use L(x) to estimate the value of g(2.5).

12. An object moves along a straight line with position function s(t), where s is in meters and t is in seconds with 0 < t < 10. The graph below represents v(t), the object's velocity function.



(a) [4 pts] Determine the intervals on which the object's position function s(t) is increasing.

(b) [4 pts] Determine intervals on which the graph of the object's position function s(t) is concave upward.

(c) [4 pts] Determine all values of t at which the position function s(t) has a relative minimum.

13. [15 pts] The dimensions of a rectangle are changing, but the rectangle's height is always twice its width. When the area of the rectangle is 50 in², the area of the rectangle is increasing at a rate of 10 in² per second. Determine the rate of change of the perimeter of the rectangle at that instant.

- 14. You plan to make a box with a square base and lid, with largest possible volume, and with surface area 140 in². Note: The last part of this problem is on the next page.
 - (a) [10 pts] If the square base of the box is x inches wide, determine a formula for the function V(x) representing the volume of the box (in cubic inches). Your function should contain the variable x and cannot contain any other variables.

(b) [5 pts] Determine a domain for V(x) which makes sense in the context of the scenario. Briefly explain why you chose the domain you provided.

The problem continues on the next page.

Problem 14, continued:

(c) [10 pts] Determine the largest possible volume of such a box. You must use calculus to verify that the volume you find is the largest possible volume.

This page is extra space for work. Do not detach this page. If you want us to consider the
work on this page, you should print your name, instructor and class meeting time below. For
the problems where you want us to look at this work, please write "see last page" next to your
work on the problem page so that we know to look here.

Name (print): ______ Instructor (print): _____

Class Meeting Time: _____